

Agency Problem of Outside Finance and Capital Structure

Overview of the lecture:

- Agency Problem of outside finance and “credit rationing” (Jensen and Meckling (1976), Tirole, ch. 3.2)
- Debt finance as the way to mitigate credit rationing (Jensen and Meckling (1976), Tirole, ch. 3.4.3, 3.5)
- Cost of debt: Risk-Shifting (Asset Substitution) Problem (Jensen and Meckling (1976))

NATURE OF THE AGENCY PROBLEM

- Investors provide funds to insider (entrepreneur or manager) as well as (some) de facto decision rights.
- How do the investors ensure that insiders
 - make value-increasing decisions?
 - pay a return on investment?

Agency Problem: insider cannot fully commit to both things; hence, investors may be reluctant to provide finance.

For example, insider can:

- – Engage in “empire building” (overinvestment)
 - Do self-dealing transactions with related parties (e.g. sell assets at below market prices to affiliated companies)
 - Resist a value-increasing takeover
 - Derive “perks”: company jets, fancy offices, etc...
 - Simply underprovide effort

MODEL OF THE AGENCY PROBLEM (CREDIT RATIONING)

Three dates ($t = 0, 1, 2$), no discounting, everybody is risk-neutral

An entrepreneur has a project and he is key to the project (nobody else can do it)

- At $t = 0$: Financing
 - Need $I > 0$
 - Entrepreneur's resources available for investment $A < I$
Hence, he needs to raise $F \geq I - A$.
 - Invests I in the project and keeps $F + A - I$.
 - Competitive capital markets (meaning entrepreneur has all bargaining power, i.e investors' participation constraint is always binding)
- At $t = 1$: Moral hazard stage
 - The entrepreneur has a choice:
 - * Behave (work, take no private benefit). Private benefit $Z = 0$
 - * Misbehave (shirk, take private benefit). Private benefit $Z = B$
- At $t = 2$: Cash flow
 - $X \in \{X^F, X^S\}$ with $\Delta X = X^S - X^F > 0$
 - $\Pr [X = X^S] := p = \begin{cases} p_H & \text{if ent-r behaved} \\ p_L = p_H - \Delta p & \text{if ent-r misbehaved} \end{cases}$

Assumption (*): Behaving is efficient, i.e.

$$p_H X^S + (1 - p_H) X^F > p_L X^S + (1 - p_L) X^F + B \text{ or } \Delta p \Delta X > B$$

Denote: project value $V \equiv NPV + Z =$

$$= p X^S + (1 - p) X^F + Z - I$$

Assumption: The project's NPV is positive if entrepreneur behaves, i.e.,

$$V_{Z=0} \equiv X^F + p_H \Delta X - I > 0$$

i.e. doing project (given entrepreneur behaves) is efficient

Contract

In exchange for financing F the entrepreneur promises repayment $R(X)$: R^F if $X = X^F$ and R^S if $X = X^S$. If entrepreneur's actions (or private benefit) are contractible, parties can also set specify explicitly whether entrepreneur behaves or not.

Payoffs

- Investors always get net payoff of 0 (competitive market), i.e.
 $pR^S + (1 - p)R^F - F = 0$
- Entrepreneur gets: $p(X^S - R^S) + (1 - p)(X^F - R^F) + Z + A + F - I = V + A$

I.e., since the markets are competitive the entrepreneur gets the whole value of the project

\Rightarrow Whenever $V > 0$, the funds will be raised (Entrepreneur compares $V + A$ with A)

First Best. Contractible actions

- The entrepreneur needs to raise at least $I - A$
- He can sell a claim on X with promised repayments at $t = 2$

$$R^F \text{ if } X = X^F \quad \text{and} \quad R^S \text{ if } X = X^S$$

For instance, debt with face value K :

$$R^F = \min\{X^F, K\} \quad \text{and} \quad R^S = \min\{X^S, K\}$$

or a fraction β of equity

$$R^F = \beta X^F \quad \text{and} \quad R^S = \beta X^S$$

Assumption (for now): $X^F = 0$

- Hence all contracts are linear in cash flows: $R^F = 0$ and $R^S \geq 0$
- Thus, there is no difference between debt, equity, etc. which allows us to ignore financing choice issues for now.

Offering R^S , entrepreneur raises exactly $p_H R^S$ (competitive market)

He needs to raise at least $I - A$. Hence, R^S must satisfy:

$$\frac{I - A}{p_H} \leq R^S \leq X^S$$

$X^S p_H > I - A$ due to the assumption that $V_{Z=0} > 0$. Hence, irrespective of A , the entrepreneur can always finance the project by setting R^S satisfying the above condition

Noncontractible actions

The above result holds under the assumption that there is no moral hazard problem.

Assumption: actions are not contractible now. Hence investors cannot force entrepreneur to behave

At $t = 1$, the entrepreneur behaves iff

$$\Delta p(X^S - R^S) \geq B \quad \text{or} \quad R^S \leq R_{\max}^S \equiv X^S - B/\Delta p \quad (\text{IC})$$

But financing the project (given entrepreneur behaves) requires

$$R^S \geq R_{\min}^S \equiv (I - A)/p_H \quad (\text{IR})$$

Hence, the first best is obtained iff

$$(I - A)/p_H \equiv R_{\min}^S \leq R_{\max}^S \equiv X^S - B/\Delta p$$

or

$$p_H(X^S - B/\Delta p) \geq I - A \quad (*)$$

Tirole calls $p_H(X^S - B/\Delta p)$ “pledgeable income” – maximum amount that can be pledged to the investors.

Role for internal funds: condition (*) is more likely to be satisfied when A large.

What if $R_{\min}^S > R_{\max}^S$, i.e. (*) does not hold?

The investors' NPV if the entrepreneur misbehaves:

$$NPV_{Z=B} = X^F + p_L \Delta X - I$$

- If $NPV_{Z=B} < 0$, the entrepreneur cannot raise $I - A$, irrespective of R^S (**Credit Rationing**)
- If $NPV_{Z=B} > 0$, he can raise $I - A$ but fails to use these funds optimally (**Deviation from value maximization**)

This is a Commitment (or Time-Consistency) Problem:

- Eventually, since the markets are competitive, the entrepreneur bears all the agency cost (he gets the whole value $V + A$ if the project is financed and A if not) \Rightarrow He would like to commit to behaving. However, once some claims are sold to investors, his incentives are determined solely by the claims that he retains.

- **WAYS TO SOLVE (PARTIALLY) THE AGENCY PROBLEM**
(increase borrowing capacity, raise pledgeable income):
 - Costly commitment (monitoring, bonding)
 - Reputation
 - Collateralization
 - Diversification
 - Capital structure

Costly Commitment:

To commit to behaving, the entrepreneur is willing to pay up to:

$$V_{Z=0} - \max\{V_{Z=B}, 0\}$$

- **Monitoring** by a blockholder, a bank, an auditor, etc...
- **Bonding**: Contractual commitment not to engage in certain actions (even if potentially valuable)

BENEFITS OF DIVERSIFICATION (Diamond (1984), Tirole, ch. 4.2)

- In a perfect market there are no benefits from corporate diversification (investors can diversify themselves by investing in different projects)
- When Agency Problem exists diversification can be beneficial.
 - Main idea: entrepreneur can cross-pledge the incomes of various projects provided they are not perfectly correlated. This increases pledgeable income and, hence, makes financing (both projects) more feasible.
- Assume there are two projects, each having the same characteristics as above
- The entrepreneur's initial wealth: $2A$.
- Assume $X^F + p_L \Delta X - I < 0$: financing is unfeasible if entrepreneur is expected to misbehave

The case of no diversification

- Assume the returns of the two projects are perfectly correlated (i.e. if one is success the other one is success too and vice versa).
- Manager can behave in both (then $Z = 0$) or misbehave in both (then $Z = 2B$).
- At $t = 1$, the entrepreneur behaves iff

$$\Delta p(2X^S - R^S) \geq 2B \quad \text{or} \quad R^S \leq R_{\max}^S \equiv 2X^S - 2B/\Delta p \quad (\text{IC}_{nd})$$

Financing the project (given entrepreneur behaves) requires

$$R^S \geq R_{\min}^S \equiv (2I - 2A)/p_H \quad (\text{IR})$$

Hence, the necessary and sufficient condition for financing both projects:

$$2(I - A)/p_H \equiv R_{\min}^S \leq R_{\max}^S \equiv 2X^S - 2B/\Delta p$$

or

$$p_H(X^S - B/\Delta p) \geq I - A \quad (*)$$

Note: if you want to finance only one project, the conditions is weaker: $p_H(X^S - B/\Delta p) \geq I - 2A$

The case of diversification

- Assume correlation is not perfect. For simplicity: no correlation at all.
- Assume entrepreneur can behave in both, misbehave in both, or misbehave in either
- Four (essentially three) outcomes are possible:
 - Both projects fail: $X = 0$
 - Both projects succeed: $X = 2X^S$
 - Only one succeeds: $X = X^S$
- How can we relax the financing condition?
- Answer: reward entrepreneur only if both projects succeed; otherwise pay all return to investors. This will help raise pledgeable income
- Specifically, the contract should look as follows:
 - $R = R_0 = 0$ if no project succeeds
 - $R = R_1 = X^S$ if only one succeeds (cross-pledging)
 - $R = R_2 < 2X^S$ if both succeed

- Financing both project, given entrepreneur behaves in both, requires:

$$2p_H(1 - p_H)X^S + p_H^2 R_2 \geq 2I - 2A$$

$$R_2 \geq R_{2\min} \equiv (2I - 2A - 2p_H(1 - p_H)X^S)/p_H^2 \quad (\text{IR})$$

- Entrepreneurs prefers to behave in both projects to misbehaving in both projects iff

$$p_H^2(2X^S - R_2) \geq p_L^2(2X^S - R_2) + 2B$$

or

$$\begin{aligned} R_2 &\leq R_{2\max} \equiv 2X^S - 2B/(p_H^2 - p_L^2) = \\ &= 2X^S - 2B/(\Delta p(p_H + p_L)) \end{aligned} \quad (\text{IC}_d)$$

Hence, the necessary and sufficient condition for financing both projects:

$$p_H [X^S - Bp_H/(\Delta p(p_H + p_L))] \geq I - A$$

This condition is weaker than (*)

- Hence, diversification increases pledgeable income and makes financing more feasible

Note: We should have checked if behaving in both projects is preferred to behaving only in one. The condition is

$$p_H^2(2X^S - R_2) \geq p_L p_H(2X^S - R_2) + B$$

or

$$R_2 \leq 2X^S - B/(p_H \Delta p)$$

, which is weaker than (IC_d) .

JENSEN AND MECKLING (1976). DEBT AS A WAY TO SOLVE THE AGENCY PROBLEM OF OUTSIDE FINANCE

Main Ideas of Jensen and Meckling:

- There are conflicts of interests
 - between insiders and outside investors
 - between equityholders and debtholders
- Insider's decisions **depend** on the capital structure. Hence, MM I does not hold: operating and financing decisions are **not** independent, i.e., the size of the pie is affected by how the pie is split.
- Proper capital structure minimizes the agency costs
- For now: focus on the conflict of interest between insiders (entrepreneur) and outside investors, i.e. what we have been discussing so far

Model

Same as before except:

- $X^F > 0$, to be able to discuss financing choices (cap. structure)
- $I > X^F$, for simplicity
- $A = 0$, for simplicity

First Best: Modigliani-Miller

Financing choices are irrelevant in the absence of Moral Hazard (i.e. when entrepreneur's actions are contractible)

Say the entrepreneur chooses to raise exactly I . Then, he offers R^F and R^S such that:

$$I = (1 - p_H)R^L + p_H R^S = R^F + p_H \Delta R$$

Debt with face value $K > X^L$:

$$R^F = X^F, \quad R^S = K = X^F + \frac{I - X^F}{p_H}$$

$$\Delta R = \frac{I - X^F}{p_H}$$

The investors's then get

$$p_H K + (1 - p_H)X^F - I = 0$$

Equity: Sell a fraction β of existing shares, i.e.,

$$R^F = \beta X^F, \quad R^S = \beta X^S$$

such that $\beta = \frac{I}{X^F + p_H \Delta X}$

The investors's then get

$$p_H \beta X^S + (1 - p_H) \beta X^F - I = 0$$

Irrespective of financing, the entrepreneur receives the investment's entire $V = NPV + Z$ and the investors receive 0 (competitive capital markets):

Optimality of Debt

Irrelevance of financing choice breaks down, once actions are non-contractible.

At $t = 1$, the entrepreneur behaves iff

$$\begin{aligned} & p_H(X^S - R^S) + (1 - p_H)(X^F - R^F) \geq \\ & \geq p_L(X^S - R^S) + (1 - p_L)(X^F - R^F) + B \quad \text{or} \\ & \Delta p(\Delta X - \Delta R) \geq B \quad \text{or} \quad \Delta R \leq \Delta R^{\max} \equiv \Delta X - B/\Delta p \end{aligned} \quad (\text{IC})$$

Financing the project (given behaving) requires

$$I \leq R^F + p_H \Delta R \quad (\text{IR})$$

Necessary and sufficient condition for the existence of R^F and R^S satisfying these constraints is

$$p_H(\Delta X - B/\Delta p) + R^F \geq I \quad (**)$$

(**) is analogous to (*): LHS is pledgeable income. (**) is more likely to be satisfied when R^F is as large as possible, i.e. $R^F = X^F$. This is precisely the debt contract with face value $K = R^S > X^F$.

Debt financing is thus an optimal response to the moral hazard problem:

All projects that can be financed (e.g., with equity) can also be debt-financed but the reverse is not true.

Intuition:

The debt contract makes the entrepreneur “internalize” the consequences of his actions for the firm value. Hence, it maximizes his incentive to exert effort.

Remarks:

- In a more general model where effort affects the distribution of cash flows $F(X | e)$ over a continuum, Innes (1990) shows that debt is optimal under two conditions (see Tirole, ch. 3.6):
 - Monotone (log) Likelihood Ratio Property:
$$\frac{\partial}{\partial X} \left(\frac{\frac{\partial F(X|e)}{\partial e}}{F(X|e)} \right) > 0.$$
 - Monotonic repayment schedule: $\frac{dR(X)}{dX} \geq 0$
- In a continuous investment model (i.e. I is not fixed, Tirole ch. 3.4) optimality of debt continues to hold.
 - Additional prediction appears: firms with lower B or higher A borrow more.

JENSEN AND MECKLING (1976). COST OF DEBT: “RISK-SHIFTING” (“ASSET SUBSTITUTION”)

- Let us introduce a conflict between debtholders and equityholders
- Same model except that now moral hazard is about risk choice:
- The entrepreneur chooses between two mutually exclusive projects generating $X \in \{0, \hat{X}, 2\hat{X}\}$.

$$\Pr [\mathbf{X} = 2\hat{\mathbf{X}}] \quad \Pr [\mathbf{X} = \hat{\mathbf{X}}] \quad \Pr [\mathbf{X} = \mathbf{0}]$$

Project A:	p_1	$1 - p_1 - p_2$	p_2
Project B:	$p_1 + \Delta_1$	$1 - (p_1 + \Delta_1) - (p_2 + \Delta_2)$	$p_2 + \Delta_2$

with $0 < \Delta_1 < \Delta_2$ and $p_1 + \Delta_1 + p_2 + \Delta_2 < 1$.

Assume that Project A's NPV is positive, i.e.,

$$(1 + p_1 - p_2)\hat{X} - I > 0$$

First Best

Project B's NPV is

$$(1 + p_1 + \Delta_1 - p_2 - \Delta_2)\hat{X} - I$$

which is less than NPV of Project A, the difference being:

$$(\Delta_2 - \Delta_1)\hat{X} > 0$$

$\Rightarrow I$ should be used for Project A.

Debt Finance

Suppose that I is raised in debt with face value K .

Assume that $(1 - p_2)\hat{X} < I$, meaning that it must be that $K > \hat{X}$, i.e. default in case $X = \hat{X}$.

The entrepreneur gets a positive payoff only when $X = 2\hat{X}$. With Project A, he gets

$$p_1(2\hat{X} - K)$$

while with Project B, he gets

$$(p_1 + \Delta_1)(2\hat{X} - K)$$

\Rightarrow once I has been raised, the entrepreneur picks Project B.

- Entrepreneur is better off in state $X = 2\hat{X}$ and equally well off when $X = 0$ or $X = \hat{X}$.
- Because of **limited liability**, entrepreneur does not internalize loss in low states, but maximizes returns in the state, where he is residual claimant.
- Ultimately, cost borne by entrepreneur: investors anticipate asset substitution and hence ask for a higher face value of debt. That is, \tilde{K} is such that

$$(p_1 + \Delta_1)\tilde{K} + (1 - p_1 - \Delta_1 - p_2 - \Delta_2)\hat{X} = I$$

Nonetheless, entrepreneur keeps picking Project B.

If NPV of Project B < 0 , investors will not provide finance (market break-down).

Equity Finance

Suppose I has been raised in equity; fraction $\beta = (1 - \alpha)$ sold.

Once I raised and invested, entrepreneur receives a fraction α of the cash flows

\Rightarrow he maximizes expected cash flows

\Rightarrow undertakes Project A, i.e., no incentives to shift to Project B.

Equity finance is clearly the optimal contract because it induces no distortion in investment decisions.

Implications of Risk-Shifting (Asset Substitution) Model

- More debt when there is less risk-shifting potential: e.g.,
 - Regulated public monopolies with less managerial discretion
 - Firms in mature industries with few growth opportunities
 - Evidence on the US seem to support these conclusions
- Risk shifting incentives are higher when the firm is in financial distress since this is when limited liability becomes important (Gambling for Resurrection). (e.g. if $\hat{X} > K$ there would be no risk-shifting)

Mitigating Asset Substitution (except using equity finance):

- **Short-term debt** allows to renegotiate lending rate to adjust for higher risk, lessening the incentives to switch or choose high risk projects.
- **Covenants** to debt contract, e.g. prohibit investments into new, unrelated lines of business.
- **Convertible Debt** gives debtholders the option to become equityholders when returns are high \implies the entrepreneur is not the sole residual claimant when $X = 2\hat{X}$. Anticipating the conversion, he opts for Project A.
 - US evidence: highly leveraged, high-growth firms are most likely to issue convertible bonds. These firms exhibit high default risk, and hence high potential for asset substitution.

Jensen and Meckling Perspective on Capital Structure

- Capital structure is such that the sum of all agency costs are minimized.
- Hence, Jensen and Meckling (1976) conclude, optimal capital structure likely to be a mix of debt and equity.
- Agency costs encompass also costs for monitoring and bonding activities. Thus, to the extent that monitoring and bonding are useful, the equilibrium capital structure is chosen to minimize sum of **all** agency costs.

For instance, suppose under-provision of effort could be avoided by monitoring and monitoring is cheap, then firm should be all-equity financed.